Jacobi matrices and non-equilibrium statistical mechanics

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Abstract: We consider XY chain with Hamiltonian

$$\frac{1}{2} \sum_{x \in \mathbb{Z}} J_x \left(\sigma_x^{(1)} \sigma_{x+1}^{(1)} + \sigma_x^{(2)} \sigma_{x+1}^{(2)} \right) + \lambda_x \sigma_x^{(3)}$$

where initially the left (x < 0)/right (x > 0) part of the chain is in thermal equilibrium at inverse temperature β_l/β_r . The temperature differential results in a non-trivial energy/entropy flux across the chain. In this talk I will describe the link between non-equilibrium characteristics of this model and scattering properties of the Jacobi matrix $hu_x = J_x u_{x+1} + \lambda_x u_x + J_{x-1} u_{x-1}$ canonically associated to the XY chain.

This talk is based on a joint work with B. Landon and C-A. Pillet.